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Unique Continuation for a Hyperbolic Equation and its Application to Inverse Problems

A.Kh. Amirov*, **M. Yamamoto****

* Karaelmas University,
Faculty of Arts and Sciences,
Department of Mathematics,
67100 Zonguldak, Turkey
E-mail: amirov@karaelmas.edu.tr

**Department of Mathematical Sciences,
The University of Tokyo,
Komaba Meguro Tokyo 153-8914 Japan
E-mail: myama@ms.u-tokyo.ac.jp

In this work we consider the timelike Cauchy problem for the following hyperbolic equation

$$\partial_t^2 u - \sum_{i,j=1}^n a_{ij}(x, t) \partial_{ij}^2 u + \sum_{i=1}^{n+1} a_i(x, t) \partial_i u + r(x, t)u = f(x, t)$$

and the related inverse problem where $a_{ij} = a_{ji} \in C^2(Q)$, $a_i, r \in L_{loc}^\infty(Q)$, here we use the following notations:
 $x = (x_1, \dots, x_n) \in \Omega \subset \mathbb{R}_x^n$, $t = x_{n+1} \in (-T, T)$, $\partial_{n+1} = \partial_t = \frac{\partial}{\partial t}$, $\partial_t^2 = \frac{\partial^2}{\partial t^2}$, $\partial_i = \frac{\partial}{\partial x_i}$, $\partial_{ij}^2 = \frac{\partial^2}{\partial x_i \partial x_j}$, $1 \leq i, j \leq n$.