## BASIC THEOREMS OF THE THEORY OF PRE-ENDS FOR SPACE DOMAINS

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In the article, we present two constructions based on the theory of preends for domains in the Euclidean space  $\mathbb{R}^n$ . The former, using factorization of a set, allows us to compactify every domain in  $\mathbb{R}^n$  homeomorphic to a ball. Applying the latter, we obtain the Hausdorff completion of a domain. As a result, we establish some analogs of the Carathéodory theorem on the boundary behavior of quasi-isometries.

*Key words and phrases*: pre-ends, quasi-isometry, intrinsic metric, boundary element of a domain, extension of a mapping.

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