THE BOUNDARY BEHAVIOR OF FUNCTIONS OF SOBOLEV SPACES DEFINED ON A PLANAR DOMAIN WITH A PEAK VERTEX ON THE BOUNDARY

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Let G be a domain with piecewise smooth boundary ∂G and with vertices of exterior peaks on the boundary and let k functions f_1, \ldots, f_k (k is a nonnegative integer) be given on ∂G .

We find necessary and sufficient conditions for existence of a function $F \in W_p^l(G)$, where $1 and <math>l \ge k + 1$ is an integer, such that $\frac{\partial^r F}{\partial N^r}\Big|_{\partial G} = f_r, r = 0, 1, \dots, k$, with N a unit vector field defined on ∂G and nontangent to ∂G .

Key words and phrases: Sobolev space, exterior peak, trace on the boundary, trace space.

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