

**ALGEBRAIC PROPERTIES OF COVARIANT  
DERIVATIVE AND COMPOSITION OF  
EXPONENTIAL MAPS***A. V. Gavrilov*

We consider the problem of calculating the Taylor series for a function  $h_x T_x X \times T_x X \rightarrow T_x X$  defined by the composition of exponential maps, where  $X$  is a smooth manifold with affine connection and  $x \in X$ . We show that the homogeneous summands of such a series can be derived by applying the Lie bracket and covariant derivative to the arguments of the function which are extended to vector fields.

*Key words and phrases:* affine connection, composition of exponential maps, nonassociative algebra.

*Gavrilov Aleksej Vladimirovich*  
Institute of Computational Mathematics  
and Mathematical Geophysics,  
630090 Novosibirsk, RUSSIA.  
E-mail: gavrilov@lapasrv.sccc.ru

Received  
May 11, 2005

Translated into English:

*Siberian Advances in Mathematics*, V. 16, N 3, 54–70 (2006).