

THE TRACES OF BESSEL POTENTIALS ON REGULAR SUBSETS OF CARNOT GROUPS

S. K. Vodop'yanov and I. M. Pupyshchev

We prove the direct theorem on the traces of the Bessel potentials L_p^α defined on a Carnot group, on the regular closed subsets called Ahlfors d -sets. The result is convertible for integer α , i.e., for the Sobolev spaces W_p^α (the converse trace theorem was proven in [1]). This theorem generalizes A. Johnsson and H. Wallin's results [2] for Sobolev functions and Bessel potentials on the Euclidean space.

Key words and phrases: Sobolev space, Bessel potentials, Carnot group, embedding theorem, trace of a function.

Vodop'yanov Sergej Konstantinovich
Sobolev Institute of Mathematics,
Novosibirsk, 630090 Russia.
E-mail: vodopis@math.nsc.ru

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Pupyshchev Il'ya Mikhajlovich
Novosibirsk State Technical University,
Novosibirsk, 630092 Russia.
E-mail: iluxa1@ngs.ru

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1. *Vodop'yanov S. K. and Pupyshchev I. M.* (2007) Traces of Sobolev functions on the Ahlfors sets of Carnot groups, *Sibirsk. Mat. Zh.* v. 48, N 6, 1201–1221 (Translated from Russian: (2007), *Siberian Math. J.* v. 48, N 6, 961–978.)

2. *Johnsson A. and Wallin H.* (1984), Function spaces on subsets of \mathbb{R}^n , *Math. Rep. Ser. 2.* v. 1, 1–121.