

**ORTHOGONAL SERIES AND LIMIT THEOREMS
FOR CANONICAL U - AND V -STATISTICS OF
STATIONARY CONNECTED OBSERVATIONS**

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The limit behavior is studied for the distributions of normalized U - and V -statistics of an arbitrary order with *canonical* (degenerate) kernels, based on samples of increasing sizes from a stationary sequence of observations satisfying φ -or α -mixing. The corresponding limit distributions are represented as infinite multilinear forms of a centered Gaussian sequence with a known covariance matrix.

Key words and phrases: stationary sequence of random variables, mixing, multiple orthogonal series, canonical U - and V -statistics.

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