

## STABILITY THEOREMS AND THE SECOND-ORDER ASYMPTOTICS IN THRESHOLD PHENOMENA FOR BOUNDARY FUNCTIONALS OF RANDOM WALKS

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In Section 1, we prove stability theorems for a series of boundary functionals of random walks. In Section 2, we suggest a new simpler proof of the theorem on threshold phenomena for the distribution of the maximum of the consecutive sums of random variables. In Section 3, we find the second-order asymptotics for this distribution under the assumption that the third moments of the random variables exist.

*Key words and phrases:* random walks, boundary functionals, stability theorems, threshold phenomena, second-order asymptotics, asymptotic expansions.

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