## THE CENTRAL LIMIT THEOREM FOR MARKOV CHAINS WITH GENERAL STATE SPACE

## S. V. Nagaev

We consider a Markov chain with general state space and an embedded Markov chain sampled at the times of successive returns to a subset  $A_0$ of the state space. We assume that the latter chain is uniformly ergodic but the original Markov chain need not possess this property. We develop a modification of the spectral method and utilize it in proving the central limit theorem for the Markov chain under consideration.

*Key words and phrases*: central limit theorem, Markov chain, transition function, space of complex-valued measures, spectral method, resolvent, kernel of an operator.

| Nagaev Sergej Viktorovich         | Received       |
|-----------------------------------|----------------|
| Sobolev Institute of Mathematics, | July 31, 2017  |
| Novosibirsk, 630090 Russia.       | Revised        |
| E-mail: nagaev@math.nsc.ru        | April 9, 2018  |
|                                   | Accepted       |
|                                   | March 22, 2018 |

Translated into English:

Siberian Advances in Mathematics, V. 28, N 4, 265–302 (2018). DOI: 10.3103/S1055134418040028

© S. V. Nagaev; 2018